

Likelihood, and other essentials

distributions

- Understand concept of likelihood and its role in assessing the strength of evidence for competing models.
 - Understand how to derive likelihood functions for diverse models.
- Work through examples on using likelihood

Excellent review of statistical
distributions can be
found at:

- <http://www.stats.gla.ac.uk/steps/glossary/>

event.

Using the multiplication rule, gives
Bayes' Theorem in its simplest
form:

- Using the Law of Total Probability:
- $P(A | B) = P(B | A).P(A)P(B | A).P(A) + P(B | A').P(A')$
- where: $P(A)$ = probability that event A occurs $P(B)$ = probability that event B occurs $P(A')$ = probability that event A does not occur $P(A | B)$ = probability that event A occurs given that event B has occurred already $P(B | A)$ = probability that event B occurs given that event A has occurred already $P(B | A')$ = probability that event B occurs given that event A has not occurred already

the number of successes in a series of trials, for example, the number of 'heads' occurring follow a Binomial distribution with parameters n and p, written $X \sim \text{Bi}(n,p)$ or $X \sim \text{B}(n,p)$, if it

... p = success probability; $0 < p < 1$

assumptions:

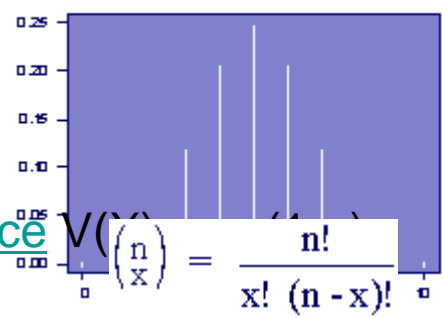
1. trials are independent; success and failure;

2. trials are independent;

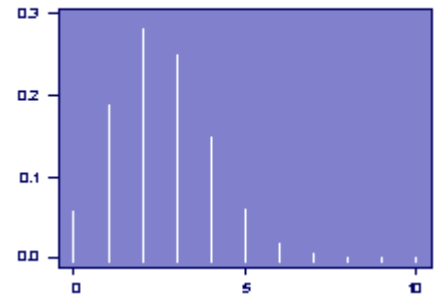
3. trials are identical.

4. mean $E(X) = np$ and variance $V(X) = np(1-p)$

Binomial (n=10, p=0.5)
Probability Density Function



Binomial (n=10, p=0.25)
Probability Density Function



$$\binom{n}{x} = \frac{n!}{x! (n-x)!}$$

$$P(X = x) = \binom{n}{x} p^x (1-p)^{n-x}$$

Binomial Distribution: discrete events that can take on two values (heads or tails, live or die, present or absent, etc).

$$P(X = x) = \binom{n}{x} p^x (1-p)^{n-x} \quad \text{mean} = np$$

$$\text{variance} = np(1-p)$$

$$\binom{n}{x} = \frac{n!}{x! (n-x)!}$$

n = number of trials, p = probability of “success”, x = number of successes.

